

# Theoretical basis for the surface spectral reflectance relationships used in the MODIS aerosol algorithm

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**Abstract:** The analysis of data from the MODIS instrument on the Terra platform to derive global distribution of aerosols assumes a set of relationships between the blue,  $\rho_{\text{blue}}$ , the red,  $\rho_{\text{red}}$ , and 2.1 micrometers,  $\rho_{2.1}$ , spectral channels. These relations have been established from a series of measurements indicating that  $\rho_{\text{blue}} \sim 0.5 \rho_{\text{red}} \sim 0.25 \rho_{2.1}$ . Here we use a model to describe the transfer of radiation through a vegetation canopy composed of randomly oriented leaves to assess the theoretical foundations for these relationships. The influence of varying fractional vegetation coverage is simulated simply as a linear combination of pure soil and pure vegetation conditions, also known as Independent Pixel Approximation (IPA). Calculations for a wide range of leaf area indices and vegetation fractions show that  $\rho_{\text{blue}}$  is consistently about 1/4 of  $\rho_{2.1}$  as used by MODIS for the whole range of analyzed cases, except for very dark soils, such as those found in burn scars. For its part, the ratio  $\rho_{\text{red}}/\rho_{2.1}$  varies from less than the empirically derived value of 1/2 for dense and dark vegetation ( $\rho_{2.1} < 0.1$ ), to more than 1/2 for bright mixture of soil and vegetation. This is in agreement with measurements over uniform dense vegetation, but not with measurements over mixed dark scenes. In the later case, the discrepancy is probably mitigated by shadows due to uneven canopy and terrain on a large scale. It is concluded that the value of this ratio should ideally be made dependent on the land cover type in the operational processing of MODIS data, especially over dense forests.

## 1. Introduction

A new generation of space-borne Earth observation instruments has been launched and can be used to monitor aerosols over land. Satellite sensors differ in their measurement capability: MODIS on the Terra satellite is using a wide spectral range (0.47 to 2.1  $\mu\text{m}$ ) to derive the aerosol optical thickness and properties [Kaufman *et al.*, 1997a]; MISR, also on Terra, retrieves aerosol properties using a modest spectral range (0.44 to 0.86  $\mu\text{m}$ ) but observing the Earth from nine different directions simultaneously along the satellite track [Diner *et al.*, 1989, 1998]. The POLDER instrument, operating in 1996-1997, using the same spectral range, observed the Earth from a wide range of angles in two dimensions and derived the aerosol properties with the help of polarization. The ATSR instrument combines 4 spectral channels (0.55 to 1.65  $\mu\text{m}$ ) with two view directions [Veefkind, 1998]. In all these instruments the measured signal consists of sunlight reflected by both the Earth surface and the aerosol layer. Some assumptions about the surface reflectance properties and aerosol properties have therefore to be made to separate the aerosol contribution to the signal from that of the surface. Each instrument takes advantage of its unique configuration to derive useful information on atmospheric aerosols.

In this paper, we concentrate on the MODIS technique based on the assumption that the ratios of the surface reflectances in the blue (0.47  $\mu\text{m}$ ) and red (0.67  $\mu\text{m}$ ) to the reflectance at 2.1  $\mu\text{m}$  are constant in space and time at the fixed values of 0.25 and 0.50, respectively. Our simulations were carried out at 0.44  $\mu\text{m}$ , which has similar characteristics to the MODIS 0.47  $\mu\text{m}$  channel. This ratio was established using remote sensing measurements in the United States [Kaufman *et al.*, 1997b] and confirmed in an independent experiment in Israel [Karnieli *et al.*, 2001]. The global application of the technique [Chu *et al.*, 2001] shows that the method works well in most cases. However no theoretical basis for this assumption had been developed so far. More specifically, the MODIS technique is based on the fact that sub-micrometer aerosol particles are transparent at 2.1  $\mu\text{m}$  (i.e., smoke and pollution but not dust). The MODIS algorithm first considers the reflectance at 2.1  $\mu\text{m}$  at the top of the atmosphere, and then uses this reflectance value to estimate the surface reflectance in the blue and red channels, using the empirical relationships described above. The aerosol optical thickness and properties are derived directly from the measured excess reflectance in the blue and red channels. In this paper, we provide some theoretical basis in support of the fixed spectral ratio approach, using surface bi-directional reflectance model of Gobron *et al.* [1997].

## 2 Model simulations

We simulate the angular and spectral properties of fully and partially vegetated surface using the plant canopy radiation transfer model developed by Gobron *et al.*, [1997]. This model solves the radiation transfer problem in the case of finite-size oriented leaves uniformly distributed over a scattering soil. The leaves are not clumped into trees, but are distributed in the space as illustrated in Fig. 1. The model computes the Bidirectional Reflectance Factors (BRFs) for mixed surfaces using a linear mixing approach:

$$\rho_{\text{mixed}}(\Omega_o, \Omega) = \sum_i f_i \rho_i(\Omega_o, \Omega) \quad (1)$$

Here,  $f_i$  is the relative fraction of the pixel area occupied by surface type  $i$ . Allowed surface types include either vegetation with a given leaf area index (LAI) or soils, while  $\Omega_o$  and  $\Omega$  denote the solar illumination and satellite observation directions, respectively. Table 1 summarizes the leaf and soil spectral properties. The latter were extracted from the database of Price [1995] and represent a wide range of actual soils. The leaf spectral properties are based on the leaf model of Jacquemoud and Baret [1990] for typical standard conditions of chlorophyll concentration and water content in a healthy leaf. The radiative transfer model has been extensively evaluated and tested against a set of three-dimensional models [Pinty *et al.*, 2001]. It was shown to be one of the best performing models within the structurally homogeneous model category. The linear

assumption used in eq. 1 to represent the angular reflectance of mixed pixels has been proven to be quite accurate for medium to low spatial resolution sensors. The calculations are performed for a wide range of leaf area index (0.05 to 5), vegetation fraction (0.25 to 1), view zenith angle (0° to 40°) and solar zenith angle (1° to 51°). The relative azimuth between the Sun and the observer is 0°, 90° or 180°.

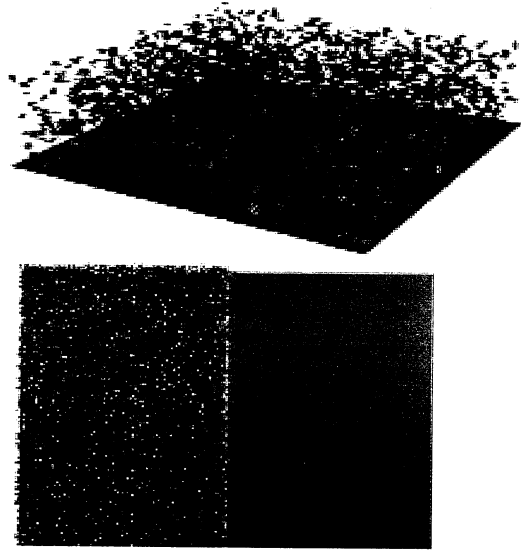


Figure 1: Artist view of the structurally homogeneous leaf distribution implemented by the canopy radiation transfer model (top), and of the mixed surfaces used in our simulations, here for a fractional vegetation cover of 50% (bottom).

Table 1: Spectral properties of leaves and soils used in the simulations

| Reflective surface / wavelength | 0.44 $\mu\text{m}$ | 0.67 $\mu\text{m}$ | 2.1 $\mu\text{m}$ |
|---------------------------------|--------------------|--------------------|-------------------|
| Leaf reflectance                | 0.054              | 0.054              | 0.148             |
| Leaf transmittance              | 0.005              | 0.014              | 0.172             |
| Dark soil reflectance           | 0.068              | 0.126              | 0.140             |
| Medium soil reflectance         | 0.102              | 0.238              | 0.357             |
| Bright soil reflectance         | 0.139              | 0.351              | 0.536             |

### 3. Results

The plant canopy radiation transfer model [Gobron *et al.*, 1997] is used to calculate the spectral reflectance of mixed scenes using eq. 1, where  $f_v$  represents the fractional vegetation cover ( $f_v = 0.25, 0.5, 0.75$  and  $1.0$ ) and  $(1 - f_v)$  is the fractional soil cover. The leaf area index (LAI) varies from 0.05 to 5. Throughout the ensemble of simulations, the vegetation density ( $f_v \cdot \text{LAI}$ ) thus varies from 0.01 to 5. Note that shadows due to variability of the height of vegetation and terrain relief are not accounted for in these calculations. We shall evaluate the implications of this issue in the discussion section. Figure 2 shows scatter plots of the simulated mixed surface reflectance at 0.44  $\mu\text{m}$  and 0.67  $\mu\text{m}$  as a function of the reflectance at 2.1  $\mu\text{m}$  for all cases corresponding to medium and bright soils. The vegetation density is represented in color, ranging from dark green for  $f_v \cdot \text{LAI} = 5$  to red for  $f_v \cdot \text{LAI} = 0.01$ . Lines corresponding to the ratios of 1/4 and 1/2, for the blue and red respectively, as assumed in the MODIS algorithm [Kaufman *et al.*, 1997a] are

superimposed. Quasi-linear relationships are observed between the blue (0.44  $\mu\text{m}$ ) or red (0.67  $\mu\text{m}$ ) and the 2.1  $\mu\text{m}$  channels for a wide range of simulated conditions. The simulated 0.44 to 2.1  $\mu\text{m}$  ratio closely follows the assumed ratio of 1/4 over the whole range of surface reflectance values. In the case of the 0.67 over 2.1  $\mu\text{m}$  ratio, however, the simulated ratios are lower than 1/2 for dark surfaces and larger than 1/2 for bright surfaces. The figure shows a transition from ratios  $\rho_{\text{red}}/\rho_{2.1}$  around 0.25 for dense dark vegetation (typically forest), to ratios larger than 1/2 for bright soils (see Table 1). In fact, measurements do show that for dense homogeneous forests the relationship between the reflectance in the 0.44, 0.67 and 2.1  $\mu\text{m}$  is such that  $\rho_{\text{blue}} \sim \rho_{\text{red}} \sim 0.5\rho_{2.1}$  [Remer *et al.*, 2001; Gatebe *et al.*, 2001], as predicted by the model. For mixed dark scenes, however the measurements show that  $\rho_{\text{blue}} \sim 0.5 \rho_{\text{red}} \sim 0.25 \rho_{2.1}$  [Kaufman *et al.*, 1997a; Karnieli *et al.*, 2001].

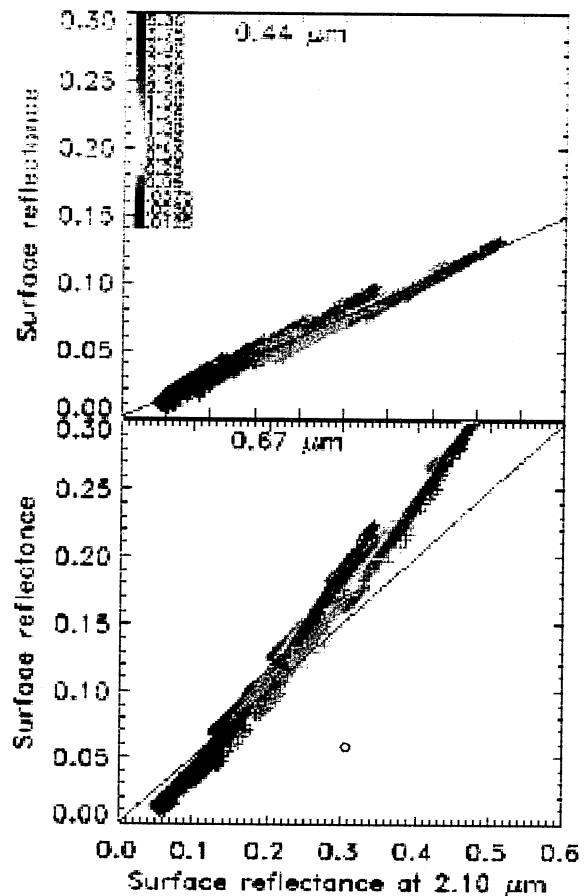


Figure 2: Scatter plots of the simulated mixed surface reflectance at 0.44  $\mu\text{m}$  (top) and 0.67  $\mu\text{m}$  (bottom) as a function of the reflectance at 2.1  $\mu\text{m}$  for medium and bright soils. The vegetation density is represented by the color bar, varying from dark green for  $f_v \cdot \text{LAI} = 5$  to red for  $f_v \cdot \text{LAI} = 0.01$ .  $f_v$  is the vegetation fraction, and LAI is the leaf area index. Lines for the ratio of 1/4 and 1/2, assumed in the MODIS algorithm [Kaufman *et al.*, 1997a] are also shown.

Figure 3 shows similar calculations to those of Fig. 2, but this time including simulations with dark soils. The plots are for a limited reflectance range of 0 to 0.2 to emphasize the range that is used by the MODIS analysis. Note also that the color bar indicates the various LAI values instead of the vegetation density ( $f_v \cdot \text{LAI}$ ). As already shown in Table 1, dark soils reduce the reflectance at 2.1  $\mu\text{m}$  much more than in the red or blue wavelengths, thus resulting in a much steeper slope. Such dark soil conditions are typical, for instance, of recent burn scars. Other soil conditions intermediate between dark and medium, would probably end up with a series of different slopes.

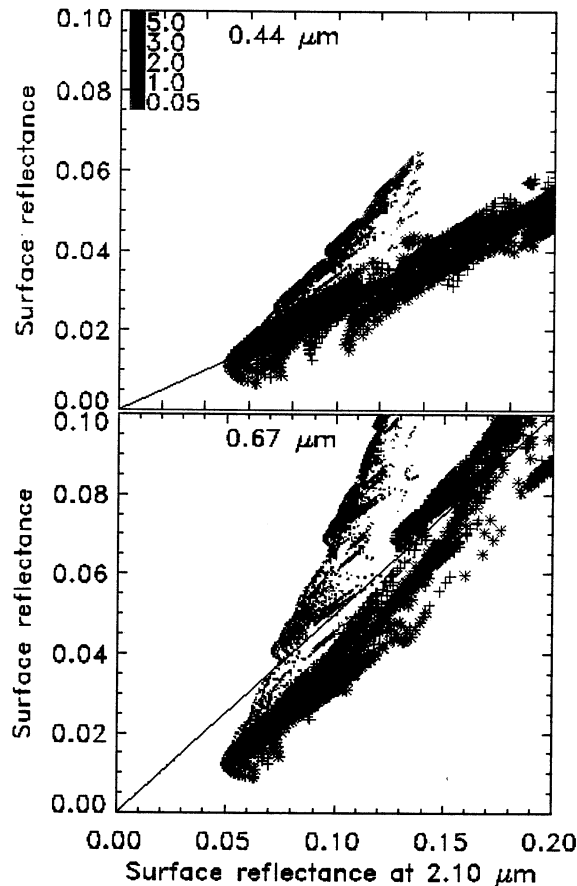


Figure 3: Similar calculations to those in Fig. 2, but including the dark soil reflectance (dots) from Table 1. The scale of the surface reflectance is limited here to a lower range of 0 to 0.2. The colors represent the leaf area index, LAI, which varies from 0.05 to 5. For each LAI value, the vegetation fraction varies from 0.25 to 1.0.

It is interesting to see whether the ratios of Fig 2 depend on the view and solar illumination directions. The ratios of the blue and red reflectances to the 2.1  $\mu\text{m}$  reflectance are shown in Fig. 4 for two solar zenith angles: 21° and 51°, representing conditions of high and low Sun. They are represented as a function of the view zenith angle. The figures correspond to full and half fractional vegetation covers, for LAI varying from 0.05 to 5 and for conditions where the reflectance at 2.1  $\mu\text{m}$  is less than 0.25. It can be seen that the ratios are weakly dependent on

the view zenith angle for low solar zenith angle. They are also weakly dependent on view zenith angle for vegetation mixed with soil. The dependence is stronger for higher solar zenith angles over full vegetation cover. MODIS will encounter high solar zenith angles at high latitudes, e.g., over the boreal forests.

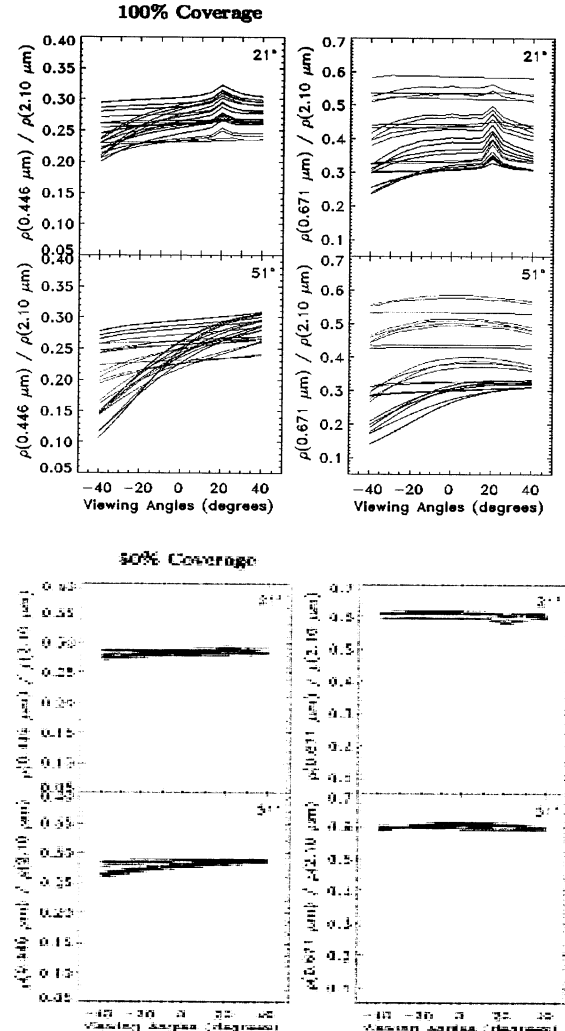


Figure 4: Ratios of the blue (0.44  $\mu\text{m}$ ) and red (0.67  $\mu\text{m}$ ) reflectances to the 2.1  $\mu\text{m}$  reflectance, represented as a function of the view zenith angle for solar zenith angles of 21° and 51°, typical of high and low Sun. The figures are given for full (top) and half fractional vegetation cover (bottom), for conditions where the reflectance at 2.1  $\mu\text{m}$  is less than 0.25. The LAI varies from 0.05 to 5 following the color convention used in Fig 3.

#### 4. Discussion and conclusions

A model describing the transfer of radiation through a vegetation canopy composed of randomly oriented leaves is used to formulate a theoretical basis for the empirical relationship between the surface reflectances in the blue, red and

2.1  $\mu\text{m}$  channels assumed in the MODIS aerosol algorithm. The calculations were carried out for a wide range of leaf area index and vegetation fractions, using a linear mixing between vegetation and soil reflectances.

We show that the reflectance in the blue is consistently 1/4 of the reflectance at 2.1  $\mu\text{m}$  for all analyzed cases over medium and bright soils. This finding extends the limited empirical basis of the MODIS aerosol algorithm to many environments found around the globe.

The ratio of the reflectance in the red to that at 2.1  $\mu\text{m}$  varies from slightly less than the empirical value of 1/2 for dense and dark vegetation ( $\rho_{2.1} < 0.1$ ), to slightly more than 1/2 for situations involving vegetation mixed with bright soils. This is in agreement with aircraft measurements over uniform dense vegetation [Remer et al., 2001, Gatebe et al., 2001] and over exposed soils but not for cases where vegetation is mixed with dark soils. One possible explanation for the differences for mixed scenes is the effect of shadows in an uneven terrain or uneven height of vegetation. Neither effect is explicitly included in the present model calculations. For example, a reflectance at 2.1  $\mu\text{m}$  of  $\rho_{2.1}=0.1$  corresponds to a surface reflectance of  $\rho_{\text{red}}=0.035$  in Fig. 2 or 3. However using values from Fig. 2 we can construct a surface cover with a combination of 60% of dark surface ( $\rho_{2.1}=0.06$  and  $\rho_{\text{red}}=0.015$ ) with 40% of bright surface ( $\rho_{2.1}=0.30$  and  $\rho_{\text{red}}=0.18$ ). If this combination is 35% shadowed and if these shadows are totally black in both channels, the linearly composited reflectance gives the same reflectance at 2.1 ( $\rho_{2.1}=0.10$ ) but higher reflectance in the red of  $\rho_{\text{red}}=0.052$ , than the original value of  $\rho_{\text{red}}=0.035$ .

Nevertheless, and in agreement with the mentioned aircraft measurements, the conclusion of this study is that for very dark surfaces (e.g.,  $\rho_{2.1} \leq 0.06$ ) the surface reflectance in the red channel, may be overestimated by assuming a ratio of 1/2, resulting in an underestimate in the derived aerosol optical thickness. A smaller ratio should be used however more extensive field and modeling experiments have to be conducted in order to better quantify this ratio.

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## **Popular Summary**

We derive routinely the concentration of aerosol particles, their properties and effect on solar radiation from satellite data, namely the MODIS instrument on the Terra platform. Aerosol is the haze part of urban pollution, smoke forest fires or desert dust. The aerosol information is derived over ocean and land. While ocean is uniformly dark and thus easy background to see the reflection of sunlight from the aerosol, the problem is more complex over the land. MODIS detects sunlight reflected both by the land surface and by the aerosol. How to distinguish between them?

We found that pollution and smoke aerosol is transparent at long invisible solar wavelengths. We therefore can use them to see how what the surface is composed of without aerosol interference, and try to use this information to guess how reflective the surface is in the visible part of the spectrum. Inferring the surface reflection of sunlight in the visible from the long wavelengths is based on collection of many measurements in different parts of the world that we did before the launch of MODIS. However we never had a clear physical understanding of this method. In this paper we for the first time use a model that simulates surface reflection across the solar spectrum for mixtures of soils and vegetation. We prove that our relationship between the surface properties in the visible and in the long wavelengths works most of the time, and found methods to correct them in cases it does not work.